Functions

PSU Math Relays 2019

- There are 33 problems
- For each problem, place your answer in the appropriate blank of the answer sheet provided.
- All functions on the test are real-valued functions.
- Simplify each answer as much as possible. Rationalize fractions. Give numerical answers in fractional form, if applicable. Do not use decimal approximations.
- Use interval notation and use $+\infty$ and $-\infty$ for positive and negative infinity.
- No calculators are allowed on the exam.
- 1. State the domain of $f(x) = x^4 + 7$ using interval notation.
- 2. State the range of $f(x) = x^4 + 7$ using interval notation.
- 3. Find the difference quotient, $\frac{f(x+h)-f(x)}{h}$, for the function $f(x) = 3x^2 5x + 17$.
- 4. Find the composition $f \circ g$ if $f(x) = 5x^3 4x + 12$ and g(x) = x 2.
- 5. Find the inverse equation of the function $h(x) = \frac{5x-1}{x+2}$.
- 6. Find the zeros of $f(x) = 6x^2 x 12$.
- 7. Find the zeros of $f(x) = x^3 + 3x^2 4x 12$.
- 8. Identify the horizontal asymptote for $g(x) = \frac{3x^2 16}{7x^2 15x 42}$.
- 9. For what positive value of x is $9^{x^2-7} = 3^{x-4}$.
- 10. What is the smallest possible value for the function $f(x) = 2x^6 + 12x^3 + 10?$
- 11. Find the product of all the real roots of $0 = 2x^3 + 3x^2 18x + 8$.
- 12. If $e^x = 3$, find e^{3x+1} .
- 13. Evaluate $f^{-1}(f(2019))$.

Recall that $a^x = y$ exactly when $\log_a(y) = x$.

- 14. Find $\log_7(49)$.
- 15. Find $\log_2(0.125)$.
- 16. Find $\log_2(.5) \log_3(81)$.
- 17. Find $2^{\log_{16}(32)}$.

For problems 18-25 below, use the functions

- $f(x) = \frac{1}{5x-9}$ • $g(x) = \sqrt{3-2x}$
- $h(x) = -x^3$

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$$k(x) = 3^{x-2}$$

Evaluate and simplify your answers. If the answer does not exist, write "DNE".

18. f(2) =19. h(-1) =20. k(0) =21. g(5) =22. (h/k)(-1) =23. $(f \circ g)(-2) =$ 24. (gk)(3) =25. $(f \circ k)(1) - (h \circ g)(2) =$

For problems 26-30 state whether the following functions are odd, even, both, or neither.

26. $y = 2 \cos x$ 27. y = 028. $y = 5x^3 - 12x^2 + 3x - 12$ 29. $y = 35x^6 + 7x^2 + 3$ 30. $y = 12x^5 + 5x^3 - 5$

For problems 31-33, use the parabolic function $h(x) = x^2 + bx + 5$, where b is a real constant.

- 31. If the axis of symmetry of the graph y = h(x) is x = 2, what is b?
- 32. If the parabola passes through the point (1, 1), what is b?
- 33. If the average rate of change for h(x) on the interval [-1, 2] is 3, what is b?