## **Functions**

## PSU Math Relays 2018

- There are 33 problems
- For each problem, place your answer in the appropriate blank of the answer sheet provided.
- All functions on the test are real-valued functions.
- Simplify each answer as much as possible. Rationalize fractions. Give numerical answers in fractional form, if applicable. Do not use decimal approximations.
- Use interval notation and use  $+\infty$  and  $-\infty$  for positive and negative infinity.
- No calculators are allowed on the exam.
- 1. State the domain of  $f(x) = x^2 + 7$  using interval notation.
- 2. State the range of  $f(x) = x^2 + 7$  using interval notation.
- 3. Find the difference quotient,  $\frac{f(x+h)-f(x)}{h}$ , for the function  $f(x)=3x^2-2x+12$ .
- 4. Find the composition  $f \circ g$  if  $f(x) = 2x^3 4x + 7$  and g(x) = x 2.
- 5. Find the inverse equation of the function  $h(x) = \frac{3x-1}{x+1}$ .
- 6. Find the zeros of  $f(x) = 2x^2 13x + 15$ .
- 7. Find the zeros of  $f(x) = x^3 2x^2 5x + 6$ .
- 8. Identify the horizontal asymptote for  $g(x) = \frac{4x^2-16}{3x^2-15x-42}$ .
- 9. For what positive value of x is  $2^{x^2-9} = 4^{3x-1}$ .
- 10. What is the smallest possible value for the function  $f(x) = x^6 + 6x^3 + 5$ ?
- 11. Find the product of all the real roots of  $0 = 2x^3 + 5x^2 11x + 4$ .
- 12. If  $e^x = 3$ , find  $e^{2x}$ .
- 13. Evaluate  $f(f^{-1}(2018))$ .

Recall that  $a^x = y$  exactly when  $\log_a(y) = x$ .

- 14. Find  $\log_6(36)$ .
- 15. Find  $\log_2(0.125)$ .
- 16. Find  $\log_3(27)\log_2(0.5)$ .
- 17. Find  $4^{\log_{16}(32)}$ .

For problems 18-25 below, use the functions

$$f(x) = \frac{1}{2x-7}$$

$$g(x) = \sqrt{5 - 2x}$$

• 
$$h(x) = x^3$$

• 
$$k(x) = 3^{x-1}$$

Evaluate and simplify your answers. If the answer does not exist, write "DNE".

18. 
$$f(2) =$$

19. 
$$h(-1) =$$

20. 
$$k(0) =$$

21. 
$$g(5) =$$

22. 
$$(h/k)(-1) =$$

23. 
$$(f \circ g)(-2) =$$

24. 
$$(gk)(3) =$$

25. 
$$(f \circ k)(1) - (h \circ g)(2) =$$

For problems 26-30 state whether the following functions are odd, even, both, or neither.

26. 
$$y = 2 \sin x$$

27. 
$$y = 0$$

$$28. \ \ y = 7x^3 - 12x^2 + 3x - 8$$

$$29. \ y = 42x^6 + 7x^2 + 3$$

$$30. \ y = 15x^5 + 5x^3 - 5$$

For problems 31-33, use the parabolic function  $h(x) = x^2 + bx + 7$ , where b is a real constant.

- 31. If the axis of symmetry of the graph y = h(x) is x = 3, what is b?
- 32. If the parabola passes through the point (1,-1), what is b?
- 33. If the average rate of change for g(x) on the interval [-1,2] is 3, what is b?