MATH RELAYS 2016 PROBABILITY & STATISTICS

Place your answer on the appropriate blank of the answer sheet. Express each answer accurate to 3 decimal places.

For problems 1-7 consider the sample data set: 5, 18, 18, 7

- 1. Find the median.
- 2. Find the range.
- 3. Find the mode.
- 4. Find the sample mean.
- 5. Find the sample variance.
- 6. Find the sample standard deviation.
- 7. Find the standard error of the mean.

For problems 8-11, consider the following discrete distribution.

X	0	1	2	3
P(X)	0.1	0.2	0.3	0.4

- 8. Find the mean of the distribution.
- 9. Find the variance of the distribution.
- 10. Find the mean of Y = -2X + 10.
- 11. Find the variance of Y = -2X + 10

For problems 12 and 13, use the following information.

x	1	2	3	4	5
У	4.63	5.40	6.18	6.56	7.48

- 12. Find the slope of the least square regression line.
- 13. Find the *y*-intercept of the least square regression line.
- 14. What is the predicted value of y when x = 2.5?
- 15. Consider two events, A and B such that P(A) = 0.35 and $P(A \cap B') = 0.17$. Find $P(A' \cup B')$.
- 16. Consider two events, A and B such that $P(A' \cap B) = 0.35$ and P(B) = 0.50. Find P(A|B).
- 17. Let A and B are two independent events such that P(A) = 0.5 and P(B) = 0.6. Find $P[A' \cap B']$.
- 18. If somebody invests \$10,000 at 3.0%, \$8,000 at 2.5%, and \$2,000 at 2%, then find the overall percentage yield. Give the answer as a percentage.
- 19. Among the 15 candidates for four positions on a city council, 7 are Democrats, 6 are Republicans, and 2 are Independents. In how many ways can the 4 councilmen be chosen so that 2 are Democrats, 1 is a republican, and 1 is an Independent?
- 20. In a lot of 10 light bulbs, there are 2 defective bulbs. An inspector selects 2 bulbs one at a time without replacement and tests them. What is the probability that both bulbs are NOT defective?
- 21. Let a container has 3 black balls and 4 white balls. All of them are identical other than the color. Randomly select three balls **without** replacement. Find the probability of getting two black balls and one white ball.

22. Let $P(X = x) = c \left(\frac{1}{3}\right)^{x-1}$ for x = 1, 2, 3, ..., and P(X = x) = 0 otherwise. Find the value of c.

23. Let
$$P(X = x) = \left(\frac{1}{2}\right)^x$$
 for $x = 1, 2, 3, ...,$ and $P(X = x) = 0$ otherwise. Let $A = \{2, 4, 6, ...\}$. Find $P(A)$.

24. If the probability mass function of a random variable X is given by

$$f(x) = \left(\frac{1}{2}\right)^x \text{ for } x = 1, 2, 3, \dots, \text{ then find the } P(X > 2).$$

25. If the probability mass function of a random variable X is given by

$$f(x) = \left(\frac{1}{2}\right)^x$$
 for $x = 1, 2, 3, ...,$ then find the $P(X > 3 | X > 1)$.

26. If the probability mass function of a random variable X is given by $f(x) = \frac{c}{x(x+1)}$ for x = 2, 3, 4, ..., then find the value of c. Note that x starts from 2.